Compilation & Program Analysis

Hype for Types

February 27, 2024

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- Common strategy for running the code: interpreter and compiler.

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Main Idea

A compiler is simply a translator from one programming language to another.

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Front End

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Front End

- **1** Parsing
- ² Elaboration (de-sugaring)

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Front End

- **1** Parsing
- ² Elaboration (de-sugaring)
- **3** Typechecking (disallow malformed programs)

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Middle/Back End **4 CPS Conversion**

¹ For more information, take 15-411 (only covers 1-3, [7-1](#page-11-0)[0\)](#page-13-0) \longleftrightarrow \longleftrightarrow \longleftrightarrow \Rightarrow

Middle/Back End

- **4 CPS Conversion**
- **5** Hoisting

¹For more information, take 15-411 (only covers 1-3, [7-1](#page-12-0)[0\)](#page-14-0)

Middle/Back End

- **4 CPS Conversion**
- **5** Hoisting
- **6** Memory Allocation

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- **Analysis/Optimizations**

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	- ▶ Dataflow Analysis
	- ▶ Often involves making a program functional (SSA form)

¹For more information, take 15-411 (only covers 1-3, [7-1](#page-17-0)[0\)](#page-19-0) λ in \mathbb{R} is a set of

Middle/Back End

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- **8** Register Allocation

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[Middle End](#page-23-0)

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Middle End - Hoisting

- **4 CPS Conversion**
- **6** Hoisting
- **6 Memory Allocation**

Move local functions to top level. But what to do with local variables?

```
let outer (x : int) =let inner (y : int) = x + y in
  inner
```
Multiple approaches!

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Middle End - Hoisting

```
let outer (x : int) : int \rightarrow int =let inner (y : int) = x + yinner
```
Straightforward solution: Partial Application $+$ Lambda Lifting

1 Turn local variables into function variables

² Introduce "partial application" structure for functions

let inner $(x : int)$ $(y : int) = x + y$

let outer $(x : int) = pApp (inner, x)$

Middle End - Hoisting

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Straightforward solution: Partial Application $+$ Lambda Lifting

1 Turn local variables into function variables ² Introduce "partial application" structure for functions

let inner $(x : int)$ $(y : int) = x + y$

let outer $(x : int) = pApp (inner, x)$

pApp (pApp (inner, 5), 6) = = > * inner 5 6

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Middle End - Memory Allocation

- **4 CPS Conversion**
- **5** Hoisting
- **6 Memory Allocation**

Create memory representations of program values:

- Primitives (ex. int)
- Functions (are values!)
- Datatypes

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Memory Allocation - Background

Stack: primitives, small program values

Heap: larger, more complicated values (ex. non-constant constructors, closures, records)

When we store something on the heap, the memory often looks something like this:

Problem

How are Algebraic Datatypes in OCaml represented in memory?

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Problem

How are Algebraic Datatypes in OCaml represented in memory?

type t = Apple | Orange | Pear | Kiwi

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Problem

How are Algebraic Datatypes in OCaml represented in memory?

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Just represent each constructor as an integer!

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Problem

How are ADTs in OCaml with arguments represented in memory?

type t = Apple | Orange of int | Pear of string | Kiwi

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 \Rightarrow

Problem

How are ADTs in OCaml with arguments represented in memory?

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The arguments could be large, so let's allocate these on the heap:

The non-parameterized constructors will remain integers, while the parameterized constructors will be pointers to memory on the heap.

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Sidenote: in OCaml the numbering for parameterized constructors is separate from non-parameterized constructors:

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Question

Why would it make sense to have separate numberings?

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Sidenote: in OCaml the numbering for parameterized constructors is separate from non-parameterized constructors:

Question

Why would it make sense to have separate numberings?

Answer: idk ask the developers (probably some optimization scheme)

type list = Nil | Cons of int * list let mylist = $Cons(1, Cons(2, Cons(3, Nil)))$

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How would mylist be represented in memory?

A linked-list!

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How would mylist be represented in memory?

A linked-list! Although this may be inefficient, so we can "unroll" to put multiple elements at one node in the linked-list.

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Question

How would mylist be represented in memory?

A linked-list! Although this may be inefficient, so we can "unroll" to put multiple elements at one node in the linked-list.

At a high level it looks something like this:

```
type list =
  Nil
 | One of int
| Two of int * int
 | Rest of int * int * int * list
```
Memory Allocation - Closures

Question

How should we represent closures?

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Memory Allocation - Closures

Question

How should we represent closures?

After lambda-lifting, all function bodies are top-level functions.

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Memory Allocation - Closures

Question

How should we represent closures?

After lambda-lifting, all function bodies are top-level functions. Function constants $=$ function pointers Closures $=$ struct with function pointer & partial application arguments (or environment map)

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Middle End - CPS

4 CPS Conversion

- **5** Hoisting
- **6 Memory Allocation**
- (deep breath) Buckle up

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[CPS Conversion](#page-46-0)

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Why CPS?

CPS conversion rewrites functions to ensure every function call is a tail call

Main Idea

CPS makes control flow explicit - everything is represented as a jump to the next continuation.

Bonus: Save stack space! Every function is tail-recursive, so no "stack overflow". (There's no "stack"!)

Remember continuations?

```
signature CONT =
sig
  type 'a cont
  val letcc : ('a cont -> 'a) -> 'aval throw : 'a cont \rightarrow 'a \rightarrow 'b
 val catch : ('a \rightarrow void) \rightarrow 'a cont
end
```
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Remember continuations?

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```

```
Γ, k : τ cont ⊢ e : τ
Γ ⊢ letcc k in e : τ
```

```
\Gamma \vdash k : \tau cont \Gamma \vdash e : \tau\Gamma \vdash \mathtt{throw} k e : \tau'
```
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Function Translation

 $\tau_1 \rightarrow \tau_2$ becomes $(\tau_1 \times (\tau_2 \text{ cont}))$ cont

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Logically $\tau_1 \to \tau_2$ is $\phi_1 \supset \phi_2$. Since continuation corresponds to classical logic, this is equivalent to $\neg(\phi_1 \wedge \neg \phi_2)$, which is $(\tau_1 \times (\tau_2 \text{ cont}))$ cont.

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val f : int \rightarrow int = fn x \Rightarrow add (x, x) where

```
add : int * int -> int
```
Function Translation

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val f : int \rightarrow int = fn x \Rightarrow add (x, x) where $add : int * int -> int$

Translates to: val f = catch (fn (x, k) => throw addCPS $((x, x), k)$) where addCPS : ((int * int)* (int cont))cont

Function Translation

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val f : int \rightarrow int = fn x \Rightarrow add (x, x) where
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```
Translates to:
val f = catch (fn (x, k)=> throw addCPS ((x, x), k)) where
addCPS : ((int * int)* (int cont))cont
```

```
To call f:
letcc (fn res \Rightarrow throw f (5, res))
```
Different IRs

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[Program Analysis](#page-56-0)

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Why Analyze Programs?

- When we write code, we write them inefficient & buggy!
- We could hand optimize & run the program and debug...

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Why Analyze Programs?

- When we write code, we write them inefficient & buggy!
- We could hand optimize & run the program and debug...
- But some optimizations/bugs can be done/caught statically!

```
void isbad () {
  int arr [150];
  int matey = 1;
  // index < 0; Bug !!
  arr[ matey -2];
  // deadcode , so we can remove this block !
  if( false ) {
     //...a lot of code...
  }
```
Dataflow

- Many program analysis problems are dataflow problems
- Dataflow is a problem where a few rules describe a relation between the variables in the construct and its neighbors

```
L1: x = 0;L2: y = 150 * 150;
L3: z = 15;L4: z = z + x + 1;L5: return x + z;
```
Dataflow

- Many program analysis problems are dataflow problems
- Dataflow is a problem where a few rules describe a relation between the variables in the construct and its neighbors

```
L1: x = 0;L2: y = 150 * 150;
L3: z = 15;L4: z = z + x + 1;L5: return x + z;
```
To analyze which variable is not used, we'll define a few dataflow rules

Neededness

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Neededness

Question

What about loops? How does our algorithm change?

Hype for Types [Compilation & Program Analysis](#page-0-0) February 27, 2024 24/27

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[Conclusion](#page-63-0)

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Summary

- Compilers are "language translators", and often compositions of smaller "language translators".
- Types guide our thinking when we implement the translations!
	- \triangleright Each language is "real", complete with types and an evaluation strategy for all well-typed programs.
	- \triangleright Bonus: we can do optimization at any point without worrying about special "invariants"!
	- \triangleright Easier to debug, too. If output code doesn't typecheck, it's a bug.
- By thinking compositionally, we slowly transform high-level code into assembly.

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Writing a compiler is very hard, but rewarding (because compilers are useful, unlike PL theory).

If this lecture seems cool, consider taking 15-411 - Compiler Design. Also beg Karl to teach take 15-417 - HOT Compilation!

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